

# WORK POWER AND ENERGY

## Q.1 Define and explain work? Also give its unit?

**Ans. work**:- when force acts on a body and body covers some distance in direction of force, then it is called work (OR) the product of force and displacement in its direction is called work. (OR) when a force displaces a body its own direction then it is called work.

**Explanation**:- work done on a body depends upon applied force and displacement covered in its direction.

i.e work done = force x displacement

$$W = \vec{f} \times \vec{s} \dots\dots\dots(i)$$

it also depends upon angle b/w force and displacement if there is any angle b/w

then eq (i) can be written as,

$$W = f \cos Q \dots\dots\dots(ii)$$

if  $Q = 0^\circ$  then  $W = f \cos 0^\circ \Rightarrow \underline{W = f \times s (1)}$  because  $\cos Q = 1$

if  $Q = 90^\circ$  then  $W = f \cos 90^\circ \Rightarrow W = f \times s \times 0 \Rightarrow \underline{W = 0}$  [ $\cos 90 = 0$ ]

if shows that work done will be equal to zero if force and displacement are perpendicular. Work is a scalar quantity and its unit is joule. If one Newton force acts on a body and displaces it to one meter then work done is equal to 1 joule.

## Q.2 Define energy? Also give its different types?

**Ans. energy**:- The ability of a body to do work is known as energy its unit same as work that is joule.

**forms of energy**:- different types of energy are given below.

- (1) **Chemical energy**:- energy which is obtained during chemical reaction and burning of substances is called chemical energy eg burning of wood coal and petroleum etc.
- (2) **Nuclear energy**:- that type of energy which produced during nuclear reaction is known as nuclear energy for example process of nuclear fission .
- (3) **Radiant energy**:- the energy of electromagnetic waves is called radiant energy . for example radio waves micro waves x – rays etc have radiant energy.
- (4) **Electrical energy**:- that type of energy with the help of which we can operate different electrical equipment is called electrical energy.
- (5) **Internal energy**:- the energy of atoms and molecules which is usually in the formula kinetic energy and potential energy is called internal energy.
- (6) **Mechanical energy**:- the energy produced by moving parts of a machine is called mechanical energy.
- (7) **Kinetic energy**:- the energy produced in a body during motion is called kinetic energy.
- (8) **Potential energy**:- energy possessed by a body by virtue of its position is called potential energy

- (9) **Heat energy**:- a form of energy which transfers from one body to another body due to difference of their temperature is called heat energy.
- (10) **Sound energy**:- the energy which gives sensation of hearing is called sound energy.

### Q.3 Define and explain kinetic energy? Also derive $K.E = \frac{1}{2}mv^2$

**Ans. Kinetic energy**:- energy produced in a body during motion is called kinetic energy (K.E)

Kinetic energy of a body depends upon mass and velocity of a body if we want to stop or move a body then the work done in this form is equal to K.E

**To prove :-  $K.E = \frac{1}{2}mv^2$  :** suppose a body of mass "m" is moving because of kicking and after covering it comes to state of rest the work done in this form is equal.

Work done =  $F \times s$  .....(i)

Now we find out values of "f" and "s" for equation (i)

We know from 2<sup>nd</sup> law :-  $f = ma$  .....(ii)

By 3<sup>rd</sup> equation of motion we can find "s"

$2as = v_f^2 - v_i^2$  .....(iii)

Now as  $v_f = 0$   $v_i = v$  and  $a = -a$  [are sign show deceleration]

$2 \times a \times s = 0^2 - v^2 \Rightarrow -2as = -v^2$

$s = v^2 / -2a \Rightarrow s = v^2 / 2a$  .....(iv)

Putting eq (ii) and eq (iv) in eq (i) we get.

Work done =  $ma \times v^2 / 2a$

Work done =  $mv^2 / 2$  OR work done =  $\frac{1}{2}mv^2$

But work done in this case appears as K.E i.e  $K.E = \frac{1}{2}mv^2$

### Q.4 defines and explains potential energy? And prove $P.E = mgh$ .

**Potential energy**: The energy possessed by a body by virtue of its position is known as potential energy (P.E).

**Explanation**:- this type of energy is produced in different cases. For example when a body is raised up to certain height or when an elastic spring is string is stretched then these bodies will possess potential energy the energy of a body by virtue of its height "h" from surface of earth is gravitational potential energy because in the case we have to do some work against gravity on lifting the object and that work appears as potential energy

**To prove:-  $P.E = mgh$  :-** suppose we have a body of mass "m" lifted to a certain height "h" from the surface of the earth as shown in fig. now on lifting the mass we have to do some work against gravity which is given by: Work done =  $F \times s$  .....(i)

Now we find out value of values of "F" and "s" for equation (i) so, we know that:-  $F = w = mg \Rightarrow F = mg$  .....(ii)

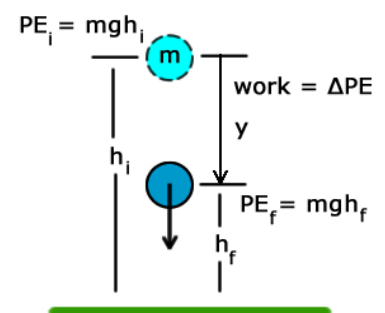
And here the distance covered "s" is equal to height "h" to which the body is raised i.e  $s = h$  .....(iii)

Now putting values of "F" & "s" in eq (i) we get

Work done =  $mg \times h$

Work done =  $mgh$

And the work done in this case appears as P.E i.e  $P.E = mgh$



**Q.5 State and explain law of conservation of energy with the help of examples?**

**Ans. Law of conservation of energy** :- this law states that energy can neither be created nor destroyed, it can be converted from one form to another form or it can be transferred from one body to another body but the total amount of energy remains constant.

**Explanation:-** Law of conservation of energy can be explained with the help of following examples.

1. A diver bends diving board because of chemical energy stored in his body and also because of this elastic potential energy stored in diving board which is then converted into kinetic energy for the diver by giving him an upward push.
2. When water is stored at certain height. Then they have P.E when these water are allowed to fall on turbines to produce electrical energy their P.E is converted to K.E.
3. A battery has chemical energy when a lamp is connected to it the chemical energy is converted to heat and light energy in the filament of lamp.

**Q.6 Explanation of law of Conservation by 2<sup>nd</sup> method.**

**Ans.** This law states that energy can neither be created nor destroyed but can be converted from one form to another form or transferred from one body to another body.

**Explanation:-** we can show it by following experiment. Let suppose we have a body of mass  $m$  which is raised up to a height  $h$  from the surface of earth. We find out its total energy at points A, B and C.

At point A:- total energy at point "A" is given by;

$$(E_t)_A = (P.E)_A + (K.E)_A \dots\dots\dots 1$$

Now P.E at A is  $mgh$  i.e.  $(P.E)_A = mg$

And as there is no motion so,  $K.E = 0$

Putting these values in eq (1) we get

$$(E_t)_A = mgh + 0 \Rightarrow (E_t)_A = mgh \dots\dots\dots (2)$$

At point B:- total energy  $(E_t)_B$  at "B" is given by

$$(E_t)_B = (P.E)_B \dots\dots\dots 3$$

Now P.E at "B"  $(P.E)_B = mg(h - x) \Rightarrow (P.E)_B = mgh - mgx \dots\dots\dots 4$

And K.E at "B"  $(K.E)_B = \frac{1}{2}mv^2 \dots\dots\dots 5$

We find value of "v" for eq (5) by 3<sup>rd</sup> eq: motion

$$2as = v^2 - v_i^2 \text{ where } a = g, s = x, v_f = v \text{ \& } v_i = 0$$

$$50, 2gx = v^2 - v_i^2 \Rightarrow v^2 = 2gx$$

Putting value of  $v^2$  in eq (5) we get

$$(K.E)_B = \frac{1}{2} m 2gx \Rightarrow (K.E)_B = mgx \dots\dots\dots (6)$$

Putting eq (4) & (6) in eq (3) we get  $(E_t)_B = mgh - mgx + mgx$

$$\text{So, } (E_t)_B = mgh \dots\dots\dots 7$$

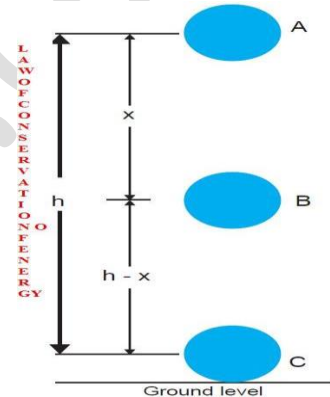
At point C :- total energy at C  $(E_t)_C$  is given by:-  $(E_t)_C = (P.E)_C + (K.E)_C \dots\dots\dots (8)$

At point C  $(P.E)_C = 0$  because object is on ground.

And  $(K.E)_C = \frac{1}{2}mv^2 \dots\dots\dots (9)$

We find v by 3<sup>rd</sup> equation of motion.

$$2as = v^2 - v_i^2$$



Putting  $a = g$ ,  $s = h$ ,  $v_f = v$ ,  $\varepsilon_i v_i = 0$  we get

$2gh = v^2$  in eq (9) we get

$$(K.E)_c = \frac{1}{2} m v^2 = mgh \quad (K.E)_c = mgh$$

Putting values of  $(p.E)$ ,  $\varepsilon (K.E)$  in eq (8) we get

$$(E_T) = 0 + mgh = (E_T)_c = mgh \dots \dots \dots (10)$$

So, from eq (2) eq (7) and eq (10) it is clear that energy does not change but remains constant.

#### Q.7 Discuss the relation b/w mass and energy?

**Ans.** Mass and energy are deeply related to each other Einstein has established the relationship between mass and energy in mathematical form according to Einstein mass and energy are interchangeable that is mass can be converted to energy and energy can be converted to mass.

Einstein mathematical relationship between mass and energy is given as:  $E = mc^2$

In “E” is energy and “m” is mass of matter where as “c” is a constant it is conservation factor which is known as velocity of light and its value is equal to  $3 \times 10^8$ /sec.

#### Q.8 discusses the electrical energy production from fuel?

**Ans.** We use different type of fuels like petrol gas and coal etc. to produce electrical energy in power station. We burn these fuel under boiler in which water is boiled where steam is produced this steam is allowed to turbines on a high pressure which rotate the dynamo and produced electrical energy.

The produced electrical energy is fed to transformer which falls or raises the level of voltage according to our desire and the transformer feed the power to transmission lines which transmit the electrical power from one place to another place i.e to cities, villages and homes.

#### Q.9 Define and explain efficiency?

**Efficiency**:- the ratio b/w output and input of a machine is called efficiency.

**Explanation**:- during the operation of a machine some energy is supplied to that machine or engine which drives it. For example we supply electrical energy to an electric motor. Similarly we supply diesel to diesel engine but it is observed that an engine cannot convert the whole input into useful work because an engine has to supply some of input energy is wasted which is transferred or radiates to the surrounding in the form of heat therefore, A machine has never 100% efficiency but less than 100% the efficiency can be found by following formula. Efficiency =  $\mathcal{M} \frac{\text{output}}{\text{input}} \times 100$

#### Q.10 Define power give its unit? Also prove that $\frac{P}{F} = \frac{v}{v}$

**Ans. Power**:- the rate of doing work is called power OR the rate of conservation of energy is called power mathematically we can write it as;

$$\text{Power} = \frac{\text{work}}{\text{time}} \Rightarrow p = \frac{w}{t}$$

$$\text{Also Power} = \frac{\text{energy}}{\text{time}} \Rightarrow p = \frac{E}{t}$$

The unit of power is watt. One watt is equal to one joule per second i.e.  $1w = 1\text{joule}/\text{sec}$

To prove that  $\frac{P}{F} = \frac{v}{v}$

As we know that;  $p = w/t \dots \dots \dots (i)$

We also know that  $w = \vec{F} \cdot \vec{x}_s \dots \dots \dots (ii)$

putting eq (ii) in eq(i) we get  $p = \vec{F} \cdot \vec{x}_s / t$

$$\Rightarrow P = \vec{F} \cdot \frac{\vec{x}_s}{t} \dots \dots \dots (iii)$$

Since  $\vec{v} = \vec{x}_s / t$  so, eq (iii) becomes as;  $p = \vec{F} \cdot \vec{v}$

# CONCEPTUAL QUESTIONS

**Q.1 for answer ( sec q 10 at page 47 ) only proof of  $\vec{P}, \vec{F}, \vec{v}$**

**Q.2 what type of energy conservation can be observed in water dams?**

The stored water in dam's possessing potential energy when these water are allowed to run turbines. The P.E of water converted to K.E when turbine runs the K.E is converted into mechanical energy. Turbines run generators which converts mechanical energy to electrical energy.

**Q.3 what happens to K.E of a bullet when it penetrates into a sand bag?**

Ans. When a bullet penetrates into a sand bag. The sand opposes its motion by a retarding force so K.E of air molecule. And some is transferred to the K.E of bullet is used against the retarding force of sand.

**Q.4 A meteor enters into earth's atmosphere and burns. What happens to its kinetic energy?**

Ans. When a meteor enters into earth's atmosphere it burns and its K.E is converted into heat and light energy. And some is transferred to the K.E of air molecule.

**Q.5 what do you understand by term energy transformation support your answer by two examples?**

Ans. Energy transformation is a process which converts energy from one form to another form its examples are given.

1. When electrical energy is given to an electric motor it converts it to mechanical energy.
2. When fuel is burnt in an engine it converts fuel energy to mechanical energy.

**Q.6 for ans( see Q9 page 46 (efficiency).**

**Q.7 for ans (see Q.5 page 45 – q.5 page 46)**

**Q.8 what kind of energy is possessed in the following cases?**

- a) A stone lying on the top of a roof
- b) Flying airplane
- c) Flying airplane
- b) A wound up spring of a toy car
- c) A speeding train?
- a) A stone lying on the top of a roof possesses gravitational potential energy
- b) Flying airplane possesses K.E energy due to motion and P.E due to its position.
- c) A wound up spring of a toy car possesses elastic P.E?

**Q.9 in each of the following situation the system consists of a ball and earth describe the work done and changes in energy forms. A) you throw a ball horizontally B) horizontally thrown by a fielder c) a ball is thrown vertically and it comes to rest at top of its flight (d) the ball back to earth where you catch?**

Ans. (a) when a ball is thrown vertically then there is no work done by gravity and no change in energy  
b) Same as (a)

- c) When a ball is thrown vertically some work is done against gravity and at the top of its flight its K.E is changes to P.E  
 d) When the ball falls back its P.E is converted to K.E and work is done by force of gravity.

**Q.10 for ans see Q8 at page 46 and compare question)**

**Q.11 which would have a greater effect on the k.E of an object doubling the mass or doubling the velocity?**

**Ans.** When mass is doubled then energy increases two times ie  $K.E \propto (2m) (v^2) \Rightarrow (K.E)_2 = mv^2$  or  $(K.E)_2 = 2 (K.E)$  when velocity is doubled then energy increases 4 times ie  $K.E \propto (m) (2v)^2 \Rightarrow (K.E)_2 \Rightarrow (K.E)_2 = 4 (K.E)$

## Numerical problems

**(1)** A 2kg object is released from rest from a height of 10m above the ground calculate:-

- The initial potential energy at the moment of release?
  - The K.E at the moment it reaches 4m above ground?
  - The speed of the object just before impact with ground?
- After the impact the object finally comes to rest? Explain what happens to the lost K.E?

**Solution:-** Mass of object =  $m = 2\text{kg}$

Height =  $h = 10\text{m}$

(1) P. E at height  $h = mgh$

$$P.E = 2 \times 10 \times 10$$

$$P.E = 200 \text{ Joules}$$

When

(2) k. E  $h = 4$

$$k.E = \frac{1}{2} mv^2 \dots\dots\dots(i)$$

we find "V" by 3<sup>rd</sup> eq of motion

$$2as = v_f^2 - v_i^2 \dots\dots(ii)$$

$$A = g = 10 \text{ m/sec}^2 \quad s = 6\text{m}$$

$$V_f = v \text{ \& } v_i = 0$$

Putting these values in eq (iii)

$$2 \times 10 \times 6 = v^2 - 0$$

$$120 = v^2 \Rightarrow v^2 = 120\text{m}$$

Putting these values in eq (i)

$$k.E = \frac{1}{2} \times 2 \times 120$$

$$k.E = 120 \text{ joule}$$

(3) speed of object according to law of conservation of energy

K.E at bottom = P.E at height

$$\frac{1}{2}mv^2 = mgh$$

$$v^2 = 2gh \Rightarrow \sqrt{v^2} = \sqrt{2gh}$$

$$v = \sqrt{2gh} = \sqrt{2 \times 10 \times 10}$$

$$v = \sqrt{200} = 14.1 \text{ m/sec}$$

(4) after impact when it comes to rest its K.E is transferred to surrounding.

**(2) In the following situation calculate the power involved?**

- (i) A force of 50N moves a body through a distance of 10m in 5 sec?  
 (ii) an object of mass 1kg is lifted up vertically through 5m in 10sec?

**Solution :-**

(i) force =  $F = 50\text{N}$        $s = 10$        $t = 5\text{sec}$        $P = ?$

As  $p = w/t \Rightarrow p = f \times s / t$

$P = 50 \times 10 / 5 \Rightarrow p = 2 \times 50 = 100$

(ii)  $m = 1\text{kg}$        $h = 5\text{m}$

$t = 10\text{sec}$       power =  $p = ?$

Now energy in this is P.E

i.e  $p = P.E/t$

$p = mgh/t$

$p = 1 \times 10 \times 5 / 10 \Rightarrow P = 5\text{w}$

**(3) A rubber ball of 0.12 kg is held at a height of 2.5m above the ground and then released**

- (i) Calculate the K.E of ball ground.  
 (ii) Calculate velocity of ball just before it hits the ground.

**Solution:-** mass of ball =  $m = 0.12\text{kg}$  height from ground =  $h = 2.5\text{m}$

(i) K.E just before lifting ground = K.E = ?

(ii) Velocity before lifting ground =  $v = ?$

(i)  $K.E = \frac{1}{2}mv^2$  ..... (i) we find out value of  $v$  by 3<sup>rd</sup> equation.

$2as = v_f^2 - v_i^2$  for which  $a = g = 10\text{m/sec}^2$   $v_i = 0$   $s = 2.5$

So,  $2 \times 10 \times 2.5 = v^2 - 0^2$

$\Rightarrow 50 = v^2$  putting value in eq (i)

$K.E = \frac{1}{2} \times 0.12 \times 50 = \Rightarrow K.E = 0.12 \times 25$

$K.E = 3\text{Joules}$

(iii) we can find velocity by 3<sup>rd</sup> eq: if motion

$2as = v_f^2 - v_i^2$

Putting  $a = g = 10$        $s = h = 2.5$        $v_f = v$        $v_i = 0$  we get

$2 \times 10 \times 2.5 = v^2 - 0^2$

$\sqrt{v^2} = \sqrt{50} \Rightarrow v = 7.1 \text{ m/sec}$

**(4) two bodies of equal masses moves with uniform velocities "v" find the ratio of their K.E?**

**Solution? :-**

$M_1 = m = m$        $v^1 = v$        $v^2 = 3v$

Ratio b/w K.E (i)  $(K.E)_1 : (K.E)_2 = ?$

We know ratio of K.E is given by:  $(K.E)_1 / (K.E)_2$  ..... (i)

Now we find  $(K.E)_1$  and  $(K.E)_2$  for eq(i), so.

$(K.E)_1 = \frac{1}{2}m_1v_1^2 \Rightarrow (K.E)_1 = \frac{1}{2}mv^2$

Also  $(K.E)_2 = \frac{1}{2}m_2v_2^2 \Rightarrow (K.E)_2 = \frac{1}{2}(m)(3v)^2$

$(K.E)_2 = \frac{1}{2}m_2v_2^2$

$(K.E)_2$  in eq (i) we get

$\frac{(K.E)_1}{(K.E)_2} = \frac{\frac{1}{2}mv^2}{\frac{9}{2}mv^2} = 1/9$

$(K.E)_1 : (K.E)_2 = 1:9$



**(5) A man whose mass is 75kg walks up a flight of 12 step each 20cm high in 5 sec find the power he develops in watts?**

**Solution:-**

Mass of man = 75kg

No of steps = 12

Hight of one step = 20cm

Hight of 12 steps =  $h = 12 \times 20 = 24 \text{ cm} = 2.4\text{m}$

Taken time =  $t = 5\text{sec}$

Power developed =  $p = ?$  As we know that  $p = \frac{E}{t}$

But energy in this case is P.E so.  $P = \frac{P.E}{t}$

$$\Rightarrow P = \frac{PE}{t} \Rightarrow p = \frac{mgh}{t}$$

$$\Rightarrow P = 75 \times 10 \times 2.4 / 5 \Rightarrow p = 75 \times 2 \times 2.4$$

$$\Rightarrow P = 360\text{w}$$

**(6) A mason of 600 N weights is climbing a loader 10m high. Find his P.E at middle of the loader.**

**Solution:-** weight of mason =  $w = 600 \text{ N}$

Hight of loader  $r = h_1 = 10\text{m}$

Hight to middle of loader =  $h_2 = 10/2 = 5\text{m}$

P.E at  $h_2 = P.E = ?$

As we know that that;

$$P.E = mgh \Rightarrow P.E = wh_2 \quad [w = mg] \\ H = h_2$$

$$\Rightarrow P.E = 600 \times 5 = 3000 \text{ joule;}$$

**(1) A ball of weight 100 N is moving on a frictionless surface with a velocity of 10m/sec complete its K.E = ?**

**Solution:-** weight of =  $w = 100\text{N} \Rightarrow m = w/g = 100/10 = 10\text{kg}$

**Velocity of moving ball =  $v = 10\text{m/sec}$**

K.E = ?

$$\text{Since } K.E = \frac{1}{2} mv^2 \Rightarrow K.E = \frac{1}{2} \times 10^5 \times 10^2$$

$$k.E = 5 \times 10 \times 10 \Rightarrow K.E = 500 \text{ joul}$$

**(8) A car of mass 800kg accelerates uniformly from rest to a speed of 25/sec in 10se what is its power?**

**Solution:-** Mas of car =  $m = 800\text{kg}$

Velocity of car =  $v = 25\text{m/sec}$

Time =  $t = 10\text{sec}$  power =  $p = ?$

As we know that  $p = \frac{E}{t}$

But energy in this case is K.E so,  $p = \frac{K.E}{t}$

$$P = \frac{\frac{1}{2} mv^2}{t} \Rightarrow p = \frac{mv^2}{2 \times t}$$

$$\Rightarrow P = \frac{800 \times 25 \times 25}{2 \times 10} \Rightarrow p = 40 \times 25 \times 25$$

$$\Rightarrow P = 25000\text{W}$$

**(9) A gril does work of 800j in lifting a 40kg bucket from a well if the acceleration due to gravity is 10/sec<sup>2</sup> calculate the depth of well?**

**Solution:-** work done = 800joul  $g = 10/\text{sec}^2$

Mass of bucket = 40 kg depth of well =  $h = ?$

The work done in this case is equal to P.E i.e

Work done =  $P.E = mgh$

$$\Rightarrow \text{Work done} = mgh \Rightarrow h = \text{work done} / mg$$

$$\Rightarrow H = 800 / 10 \times 40 \Rightarrow h = 2\text{m}$$